Labour Market Effects of Wage Inequality and Skill Biased Technical Change in Germany

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Abstract

This paper analyses the relationship between wage inequality and labour market development. Relevant economic theories are ambiguous, just as public debates. We measure the effects of wage inequality, skill-biased and skill-neutral technology on hours worked, productivity and wages in a novel structural vector error correction framework identified by non-recursive long-run restrictions. Results show that skill-biased technology shocks reduce hours worked but increase inequality, productivity and wages. Structural inequality shocks also have a negative impact on hours worked, but additionally reduce productivity. We find relevant effects of inequality both above and below the median wage.

Zusammenfassung


JEL classification: C32, I24, J24, J31

Keywords: inequality, wages, productivity, hours, SBTC, SVEC

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1 Introduction

Recent years witnessed increasing debates on economic inequality worldwide. This brings the question of the effects of inequality on economic growth or the labour market to the fore. However, as vast as the range of literature on this issue, as differing are the theoretical hypotheses and channels linking inequality to the macroeconomic variables of interest. On the one hand, there are theoretical considerations stating that wage dispersion is a necessary precondition, i.e. the price, for higher incentives, investment, growth rates and employment chances. On the other hand, a range of theories expect a higher level of inequality to impede the opportunities of an important share of the labour force to participate on educational advancement, signifying an obstacle to growth, productivity and employment development. Empirical evidence ranges from finding results in favour of the first (e.g. Forbes (2000), Bowles and Park (2005)) over ambiguous results (e.g. Persson and Tabellini (1994)) to those in favour of the latter (e.g. Panizza (2002)).

However, the lion’s share of existing research links inequality to labour market outcomes only indirectly, e.g. by investigating the effects on economic growth, investment, or political stability (see, for instance, Cingano (2014) or Alesina and Perotti (1996)). Studies that directly investigate the relationship between inequality and labour market outcomes are scarce. Fitzenberger and Garloff (2008), for example, examine the impacts of wage disparity on the level of unemployment. Furthermore, country-specific measures of inequality are available only on a yearly frequency which makes in-depth structural analyses of short-run and dynamic effects difficult. Instead, existing literature often focusses on the cross-sectional dimension via multiple country analyses (see, for instance, Forbes (2000)). Naturally, relationships for single countries cannot be inferred from these studies. Another strand of the literature (e.g. Kölling (2014)) focuses on firm level data and links wage dispersion within companies to bargaining power, productivity, the profit rate and competitiveness. However, the conclusions to be made concern employment effects at the firm’s level only and are difficult to transfer to the aggregate level.

We contribute to the literature by proposing an identification scheme of the short- and long-term effects of inequality and (skill-biased and skill-neutral) technology shocks on the labour market in a structural vector error correction (SVEC) setting. As one important issue, we seek to uncover the relationship of the overall employment level and its structure, i.e. wage inequality. We can rely on a decent number of observations at the longitudinal section using the integrated employment biographies (IEB), a unique administrative dataset by the Federal Employment Agency in Germany. The data range from 1975 to 2014 and allow us to collect labour market information of every single employee during his or her employment career. Hence, we can spot changes in overall inequality not only once per year, but at any point in time. Logically, inequality is no longer the limiting variable in terms of frequency. As a consequence, the full range of quarterly information stemming from variables such as productivity, hours or wage cost is at our disposal for an in-depth structural macroeconometric investigation.

We calculate the Gini coefficient as measure of wage inequality. The results show that the well-documented upward trend in wage inequality that prevailed for decades has come to
an end and even reversed since 2010, a result also found by Weber (2015). We find that this reversion in wage dispersion is mainly driven by a reduction of inequality in the lower half of the wage distribution.

For identification purposes, we construct a dynamic cointegrating model with non-recursive short- and long-run restrictions. The analysis is embedded in a framework including major driving forces of the labour market and inequality, productivity shocks and skill-biased technical change (SBTC). For this purpose, we residually measure SBTC from time series of the skill premium and the relative labour supply. Importantly, the ambiguity of empirical results on the effects of inequality could stem from the fact that wage dispersion itself, besides other factors, can be driven by inherently efficiency-enhancing forces, SBTC representing the prime case (see Katz and Murphy (1992) or Juhn et al. (1993), for instance). Hence, we allow the effects of structural inequality shocks on the labour market variables of interest being discriminated from the effects of SBTC.

Results based on the impulse responses show that skill-biased technology shocks increase productivity and wage costs, but reduce hours worked and drive up inequality. Structural inequality shocks also have a negative impact on hours worked, but additionally reduce productivity. Allowing for different effects of inequality below and above the median wage shows that both types of wage dispersion have negative labour market effects, somewhat stronger for the former. Furthermore, we find that (skill-neutral) technology shocks have a positive long-run effect on hours worked.

The remainder of the paper is structured as follows: Different theories linking inequality to growth or labour market variables are discussed in section 2, which also addresses the role of SBTC. Section 3 discusses the variable selection and introduces the data used in this paper. Section 4 presents our macroeconomic model, the identification strategy and the estimation procedure. The results based on the impulse responses as well as robustness checks are laid out in section 5. The last section concludes.

2 Theoretical background

2.1 Inequality effects in the literature

The following paragraphs present a short overview of the mechanisms postulated in the literature analyzing the relationship between inequality and economic growth or – though only scarcely existing – between inequality and the labour market.

Theoretical considerations consistent with the incentive hypothesis postulate that wage dispersion is a necessary precondition, i.e. the price, for higher investment, growth rates and employment chances. Mirrlees (1971) or Lazear and Rosen (1981), for instance, state that higher dispersion leads to higher incentives for harder work, more investment and higher willingness to take risks to benefit of high rates of return. This provides a direct link to aggregate productivity: High skill premia could motivate more people to improve their educational status. Given that high-education workers are more productive, aggregate productivity is influenced, too.
Another strand of the literature (e.g. Kaldor (1955)) theoretically postulates a positive relationship between inequality and growth through a different mechanism. In short, it is based on the finding that the rich have a lower propensity to consume than the poor. In this context, higher dispersion raises aggregate savings and hence more capital is accumulated. The Solow model presented in Bourguignon (1981) puts a formalized framework to this hypothesis. The author shows that there are multiple steady states each of which is associated with a different degree of inequality if savings are a convex function of income. However, the more unequal steady states are the ones with higher aggregate output.

By contrast, theories in line with the opportunities hypothesis expect a higher level of inequality to impede the opportunities of an important share of the labour force to participate on educational advancement, signifying an obstacle to employment development. Galor and Zeira (1993) formalized the so-called human capital accumulation theory. It depends on imperfect financial markets in which the level of income (or wealth) determines whether an individual can afford profitable investments. At the educational market, the poor do not receive the optimal level of education even though the rate of return on education is high. This type of under-investment is not only negative at the individual level, but also for the society, and harmfully affects future productivity and growth.

Another strand of the literature such as the endogenous fiscal policy theory (see Persson and Tabellini (1994), for example) links inequality to institutions: High wage dispersion leads voters to insist on higher tax rates, more regulation and anti-business policies all of which could harm growth through reduced incentives to invest. Related to this theory is the political instability argument. Alesina and Perotti (1996), for instance, argue that extreme inequality may lead to social unrest and hence be a drag on growth. Nel (2003)’s findings do not support this hypothesis in a clear way. He finds no statistically significant effects of inequality on political stability. However, he argues that high levels of inequality change potential investors’ risk perceptions, which negatively affects future growth prospects.

The theories presented so far link inequality to the labour market only indirectly. Studies that directly investigate the relationship between inequality and labour market variables are scarce. Bowles and Park (2005), for instance, investigate how incentives to emulate the rich influence an individual’s decision between labour and leisure, so that greater inequality can lead to longer work hours. Fitzenberger and Garloff (2008) examine the impacts of wage disparity on the level of unemployment and analyse the frictional and the heterogeneity hypothesis. The frictional hypothesis postulates that both income inequality and unemployment increase if the bargaining power of companies increases. By contrast, the heterogeneity hypothesis links the wage of an employee to his/her marginal productivity. A compression of wages, e.g. by minimum wages, leads to high employment barriers, signifying high entry rates to unemployment and low exit rates out of unemployment. The results do not clearly support either hypothesis. However, the authors state that the frictional hypothesis seems to perform better since they find no negative correlation between unemployment within age/education cells and within-cell wage dispersion.

A further competing set of theories links wage inequality to a firm’s productivity, profit rate and competitiveness (see, e.g. Kölling (2014)). In theory, there should be a positive re-
relationship among these variables if efficiency and tournament wages increase the firm’s productivity, while there should be a negative relationship if wage inequality violates fairness beliefs and reduces workers’ motivation and the firms’ attractiveness. Under the assumption that the successful companies survive while the unsuccessful ones die, one could translate these firm-level based theories into considerations at the aggregate level.

To summarize, the wide range of research trying to theoretically capture the mechanisms through which inequality impacts growth allows both negative or positive effects. Empirical work that aimed at discriminating between these channels has often been ambiguous or inconclusive. Since existing literature often focusses on multiple country analyses, relationships for single countries cannot be inferred. The ambiguity of empirical results on the effects of inequality could also stem from the fact that wage dispersion itself, besides other factors, can be driven by inherently efficiency-enhancing forces. In this context, SBTC represents the prime case in the literature (see Katz and Murphy (1992), Juhn et al. (1993), for instance). The next subsection provides a more detailed discussion on this issue.

2.2 The role of SBTC

According to Acemoglu (2002) or Moore and Ranjan (2005), amongst others, the rapid computerization at workplaces and the contemporaneous increase in wage dispersion during the past several decades is not a mere coincidence. If computers, robotics and the widespread usage of the internet complement skilled workers and replace lower skilled labor-intensive tasks, SBTC can be seen as direct source of an increasing skill premium and wage inequality.

However, inequality not only exists in terms of qualification, but alongside many other dimensions such as gender, race, regions, sectors, or age. As Card and DiNardo (2002) point out, SBTC is not able to explain the development of other dimensions of wage dispersion such as racial or gender wage gaps. Logically, inequality can be driven by other sources as well, for instance by the introduction or changes of minimum wages, by gender-, region- or sector-specific policy measures promoting or restricting certain parts of the workforce, by globalisation or by changes in the bargaining power of unions. We argue that these sources are conceptually different from SBTC since they do not directly aim at favouring the skilled over the unskilled. By the same token, SBTC has an inherent efficiency-increasing nature, distinguishing it from other sources of inequality.1

We explicitly model SBTC as source of inequality in order to isolate structural inequality shocks from technology shocks favoring the skilled over unskilled workers. This requires measuring SBTC so that it can be controlled for in our structural model. We use the theoretical framework introduced by Katz and Murphy (1992) that allows to residually infer SBTC from observable variables (such as the skill premium and the relative factor supplies) and from parameters that can be estimated (the elasticity of substitution between skilled and unskilled workers).

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1 Moore and Ranjan (2005), for instance, find that, although globalisation and SBTC both increase wage inequality, the respective shocks have different effects on the labour market.
unskilled workers). The approach borrows from Solow (1957)’s way of residually quantifying factor-neutral technical change from measures of aggregate output, capital and labour and an estimate of the elasticity of output to capital. We follow Acemoglu (2002) and provide a more general view to this framework using a constant elasticity of substitution CES production function for the aggregate economy:

\[ Y(t) = [(A_l(t)L(t))^{\rho} + (A_h(t)H(t))^{\rho}]^{\frac{1}{\rho}}, \]

where \( \rho \leq 1 \). \( L(t) \) and \( H(t) \) denote the number of low-education and high-education workers supplying labour inelastically at time \( t \), \( A_l \) and \( A_h \) are the respective factor-augmenting technology terms. The elasticity of substitution between the two factors is defined as \( \sigma \equiv 1/(1-\rho) \). Assuming competitive labour markets, the skill premium reads as follows:

\[ \frac{w_h}{w_l} = \left( \frac{A_h}{A_l} \right)^{\frac{\sigma-1}{\sigma}} \left( \frac{H}{L} \right)^{\frac{-1}{\sigma}}. \]

Taking the natural logarithm on both sides and solving for relative skill productivity yields:

\[ \ln \left( \frac{A_h}{A_l} \right) = \frac{\sigma}{\sigma-1} \left[ \ln \left( \frac{w_h}{w_l} \right) + \frac{1}{\sigma} \ln \left( \frac{H}{L} \right) \right]. \]

As Violante (2016) points out, one can directly measure SBTC from Equation (3) given an estimate of \( \sigma \), and given time series on the skill premium and relative factor supplies. In section 3 we will discuss how to feed this theoretical framework with data.

3 Variable Selection and Data

In our model of the economy and the labour market we use five variables: productivity, real wage cost, hours worked, SBTC, and inequality. We measure these variables as explained in the subsequent paragraphs. All data are either available at a quarterly frequency or are converted from monthly frequency. They range from 1975Q1 to 2014Q4 so that the total number of observations amounts to 160. For adjusting the structural level shift in 1992Q1 due to the German reunification, we could rely on an overlap of the German and West German macroeconomic time series in 1991, providing a factor that we applied to the time series after the shift. This section explains the respective data sources and methods used for data preparation.

Productivity

Productivity is both an important factor involved by the hypotheses discussed in section 2 and a key factor in modern theories of the labour market (e.g. Mortensen and Pissarides (1994)). Therefore, we include this variable in our structural model. We use seasonally adjusted productivity from the Federal Statistical Office (Destatis) in Germany.
is measured in terms of real GDP per hours worked by the whole working population (hours being described below). The solid line in Figure 1 shows the development of productivity after taking logs and multiplying by 100. Besides the normal business cycle fluctuations, the slump during the Great Recession of 2008/2009 is clearly visible.

**Wage Cost**

The second variable in our model is real wage cost as published by the Federal Statistical Office. It comprises the dependent workers’ gross wages and salaries plus the employers’ social security contributions, in relation to the hours worked by all dependent workers. The time series is seasonally adjusted and converted to real terms through the GDP deflator. The dashed line in Figure 1 shows the log × 100 of real wage cost in Germany since 1975Q1. The graph might suggest the existence of a long-run relationship between productivity and wages. Based on cointegration tests, we will allow for such a relation in our model. Cointegration between productivity and real wage cost is economically equivalent to the presence of a covariance-stationary labour share. More detailed information on our structural model is presented in section 4.

Figure 1: Productivity and real wage cost

**Notes:** The graph shows the log × 100 of seasonally adjusted productivity (solid line) in terms of GDP per hour worked (working population), and the log × 100 of seasonally adjusted real wage cost in terms of salaries and wages per hour worked (dependent workers). Nominal wage cost have been converted to real terms by usage of the GDP deflator. For both variables, the respective structural breaks in 1992 due to the German reunification have been eliminated and the respective sample means have been subtracted. Source: destatis.

**Hours**

Our preferred variable for measuring the labour market quantity effects of inequality and SBTC is total hours as calculated by the Institute for Employment Research (IAB) in Nurem-
berg. It is a holistic measure of labour market activity that, in contrast to the number of dependent workers, considers the employees’ working time and hence is able to capture structural effects such as the changing importance of the low-pay sector, part-time work or minijobs. This choice is in parallel to large strands of literature measuring influences of technical change on the macroeconomy, e.g. Gali (1999). Figure 2 shows the log $\times 100$ of seasonally adjusted hours worked by all dependent workers. It clearly mirrors the downturn of the German labour market over the 1990s and the recovery since 2005 that is interrupted only temporarily by the Great Recession.

Figure 2: Hours

Notes: The graph shows the log $\times 100$ of seasonally adjusted hours worked by all dependent workers. The structural break in 1992 due to the German reunification has been eliminated.
Source: IAB working time accounts.

Skill-Biased Technical Change

Subsection 2.2 delivers the theoretical framework for measuring SBTC. It requires observations of the skill premium and the relative factor supply which we obtain from the Sample of Integrated Labour Market Biographies (SIAB) of the IAB. This data set provides detailed information about an individual’s (un)employment history on the German labour market. Basically, SIAB is a 2 percent random sample of the population collected in the Integrated Employment Biographies (IEB) that comprises all (un)employed persons in Germany between 1975 to 2014.

Concerning wages, we rely on information from full-time workers because part-time wages cannot be pinpointed due to a lack of information about the hours worked (beyond the full-time / part-time information). In case of multiple employment, only reports of the main job are included. When determining labour supply, we count all employees and unemployed.

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2 In 2011, the format of the part-time attribute in employers' reports to social security changed. However, none of the variables relying on wage information from the IEB (i.e., SBTC and the Gini coefficient below) contains relevant shifts in this period. Logically, adjusting for breaks would leave the results unchanged.
(including participants of active labour market policy measures) with completed vocational training or higher education as being high-skilled and all workers without completed vocational training or high school degree as being low-skilled ($H$ and $L$ in Equation (3)). At first, this classification seems to differ from the college vs. no college perspective. However, for the German case we find it appropriate due to the special role of the dual system of vocational training in Germany (compare Müller and Wolbers (2003)). Indeed, it comprises the main part of jobs that require a college degree in other countries. Shifts in the labour supply variables in 1992 (reunification) and 2005 (statistical effects of the Hartz reforms) were adjusted in ARIMA models with dummies.

In order to calculate the skill premium, we run monthly Mincer-type regressions of wage on age, squared age, seniority, squared seniority and dummies for gender, nationality and East-Germany.\(^3\) Note that variables such as education, sectors or firm size are left out in the regressions. This fits the needs of our analysis since alongside these dimensions SBTC unfolds its distorting character.\(^4\) The resulting residuals from the regressions are used to calculate $w_h$ and $w_l$ of Equation (3), i.e. the average (adjusted) wages for high-education and low-education workers, respectively.

In the following, we discuss the timing of the reports in SIAB. Usually, the employer reports the individual worker’s data relevant for the social security system once per year (annual report). In this case, the reported wage reflects the total payment received by the worker during the calendar year. However, the timing of individual wage changes due to promotion or tariff changes within a year is not reflected in annual reports which leads to a substantial underestimation of the intrayear wage dynamics. This is less of a problem if a worker changes his or her job after January or before December, or if there is an intrayear switching of, say, the health insurance company. These or similar events affecting the social security system require additional reports from which the true wage dynamics within a calendar year can be deduced. This is why, in order to calculate $w_h$ and $w_l$, we use the wage information of annual reports only once per year (in January) whereas for February to December, we rely on wage information stemming from intrayear reports.\(^5\)

There is broad consensus in the literature that the elasticity of substitution between high- and low-education workers, $\sigma$, ranges between 1.4 and 2. Katz and Murphy (1992), for instance, find a value of $\sigma \approx 1.4$ for US data, whereas Angrist (1995)’s results on Palestinian skill premia imply $\sigma \approx 2$. Möller (2000)’s finding of $\sigma \approx 1.7$ for German data naturally will be our preferred estimate for this study. This value is also in accordance with other studies (see, for instance, Hamermesh (1993) or Bound and Johnson (1992)). The robustness checks in section 5.3 reveal that the resulting impulse responses are robust with respect to different elasticities of substitution.

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\(^3\) Whenever wage information stemming from SIAB or IEB is used, wages above the social security contribution ceiling are imputed following Gartner (2005). For workers who first appear in the data set in 1975 (West) or 1992 (East), the seniority variable is left-censored. Then, we proxy seniority by potential work experience according to age and education.

\(^4\) Leamer (1996), for instance, emphasize the effect of the sectoral bias in technical change on wage rates.

\(^5\) The number of workers supplying high-education or low-education labour, $H$ and $L$, is not affected since the data set mirrors the true stock of (un)employed persons at any point in time.
Notes: The graph shows the seasonally adjusted relative skill productivity $\times 100$ as measured by Equation (3). The monthly data were converted to quarterly frequency. Further information in the text. Source: SIAB.

Figure 3 shows the development of seasonally adjusted SBTC with $\sigma = 1.7$ after converting the monthly time series into quarterly data and multiplying by 100. SBTC is steepest through the 1990s but markedly flattens in the subsequent decade.

Inequality

We choose the Gini coefficient $G$ given by Equation (4) as our measure of wage inequality.

$$G = \frac{\sum_{i=1}^{N} \sum_{j=1}^{N} |w_i - w_j|}{2N \sum_{i=1}^{N} w_i},$$

where $N$ denotes the total number of cross-section individuals. Hence, $G$ is equivalent to half of the average absolute wage difference of all pairs of employees at a certain point in time, divided by the average wage in order to normalize for scale. It can take on values between 0 (in case every worker earns the same) and nearly 1 (in case all wages go to a single worker). From a different perspective, $G$ equals 2 times the area between the 45° line signifying a perfectly equal wage distribution and the actual wage distribution given by the Lorenz curve. We use the IEB as data source that allows us to collect wage information of 100 percent of the workers in order to avoid noisy fluctuations in the data. In contrast to SBTC, we use unconditional wages to measure inequality preventing us from ignoring specific sources of inequality.

The wage distribution of annual reports substantially differs from that of intrayear reports because the first is based on more stable employment episodes that often span several
years, while the latter is often based on shorter (and worse paid) employment episodes. Logically, this has an influence on the values of the Gini coefficient. For every calendar year, we choose the respective inequality value of January (which includes both all annual reports and current intra-year reports falling onto January) as anchor value around which the intra-year fluctuations from February to December are built. This combines the appropriate level of inequality that would appear in an annual time series and the full intrayear variation.

Figure 4: Inequality

Notes: The graph shows the seasonally adjusted Gini coefficient × 100 based on full time workers subject to social security contributions aged 15 to 64. Level shifts in January 1978, January 1984 and January 1992 have been eliminated. The monthly data were converted to quarterly frequency. Further information in the text. Source: IEB.

Figure 4 shows the seasonally adjusted Gini coefficient after converting the monthly time series into quarterly data and multiplying by 100. Note that, in addition to the reunification break, level shifts in 1978Q1 and 1984Q1 due to a break in the way annual special payments are reported have been eliminated as well. The figure reveals that the well-documented upward trend in wage inequality that prevailed for decades has come to an end and even reversed since 2010, a result also found by Weber (2015). The decline in inequality could be explained by the phasing out of the first wave of computerisation and the fact that the new digitalisation wave (“4.0”) did not yet start (compare also Beaudry et al. (2010) for technology waves). However, even though SBTC flattens, too, this change is clearly not big enough to account for the marked reduction of inequality. This underlines that inequality is driven by other sources as well.
4 Methodology

4.1 Model Setting

Several features of the interdependence of inequality and the labour market require specific traits of the econometric model: First, we are interested in the response of, say, hours or productivity to inequality shocks over time, so the model needs to be dynamic. Second, we want to isolate structural inequality shocks from Skill-Biased Technology (SBT) shocks which in return must be disentangled from skill neutral technology shocks. This requires a structural model to be identified by statistical and economic reasoning. The presence of technology shocks leads us to form a dynamic structural model with long-run restrictions that do not preempt the results with respect to the hypothesized effects.

The long-run and the structural dimensions will be introduced below. Regarding the dynamic model, we start with a VAR. This has the advantage to capture very general interaction of the variables without imposing strong structural assumptions a priori. The VAR with lag length $q + 1$ reads

$$y_t = c_0 + c_1 t + \sum_{i=1}^{q+1} A_i^* y_{t-i} + u_t,$$

where $y_t$ contains the $n = 5$ endogenous variables log of productivity ($p$), log of real wage cost ($w$), log of hours worked ($h$), SBT and inequality ($I$). $A_i^*$ are $n \times n$ coefficient matrices and $u_t$ is an $n$-dimensional vector of white noise errors. As deterministic terms, we allow for a $n \times 1$ vector of constants $c_0$ and a linear trend. In choosing the model size, we seek to limit the complexity and empirical requirements, while upholding economic interpretability in the sense of being able to address the core research questions.

Augmented Dickey-Fuller (ADF) tests confirm that our variables should be treated as non-stationary. However, before proceeding, assume that the labour share $(wN)/(pN)$ is covariance-stationary. This implies a cointegration relation between $p$ and $w$ as visualized in Figure 1. Indeed, this assumption is supported by an ADF test for the labour share which rejects non-stationarity on the 3 percent level. Here, we allowed for a linear trend just as in Equation (5), which might already be suggested by the time series developments in Figure 1.

In case of long-run comovement, the variables contain common non-stationary components. According to Johansen (1995), the commonness of $n - r$ such stochastic trends is reflected by a reduced rank of $A^*(1)$, with $A^*(L) = I_n - \sum_{i=1}^{q+1} A_i^* L^i$. Consequently, one can write $A^*(1) = -\alpha\beta'$, where $\beta$ spans the space of the $r$ cointegrating vectors, and $\alpha$ includes the corresponding adjustment coefficients. Granger’s representation theorem leads to the VECM

$$\Delta y_t = \alpha[\beta'y_{t-1} + c (t - 1)] + c_0 + \sum_{i=1}^{q} A_i \Delta y_{t-i} + u_t,$$
with \( A_i = -\sum_{j=i+1}^{q+1} A_j, \) \( i = 1, \ldots, q. \) Note that \( \beta' = (1 \beta_2 0 0 0) \) in our case since the cointegration involves only \( p \) and \( w. \) The linear trend with coefficient \( c^*_1 \) is restricted to the cointegration space (compare Johansen (1995)).

### 4.2 Identification

The VECM in Equation (6) represents the reduced form of an underlying structural system. In particular, the correlated residuals in \( u_t \) do not represent economically interpretable innovations. Instead, they are usually specified as linear combinations of some structural shocks. Formally, this can be written as

\[
u_t = Be_t, \tag{7}\]

where \( B \) is an \( n \times n \) parameter matrix, and \( e_t \) represents the vector of structural disturbances. \( B \) contains the initial impacts of the shocks on the respective variables, with diagonal elements normalised to be non-negative.

Evidently, \( B \) introduces \( n^2 = 25 \) unknown coefficients into the model, which cannot be determined form the reduced form without further elaboration. First, the variances of \( e_t \) are normalised to one and the cross-correlations between the different structural shocks are assumed zero (as is standard in structural VAR models). This reduces the number of unknowns by \( n(n + 1)/2 = 15, \) still leaving \( n(n - 1)/2 = 10 \) restrictions to impose for identification of the structural form. We address this issue by a set of long-run restrictions.\(^5\)

From the VECM moving average representation (Johansen (1995)) one gets the matrix of the long-run effects of the reduced-form residuals \( u_t \):

\[
\Xi^* = \beta_\perp(\alpha_\perp' (I_n - \sum_{i=1}^{q} A_i) \beta_\perp)^{-1} \alpha_\perp', \tag{8}\]

with \( \perp \) denoting the orthogonal complement (thus \( \alpha' \alpha_\perp = 0 \), where both \( \alpha \) and \( \alpha_\perp \) have full column rank). In detail, the \( i \)th row of \( \Xi^* \) contains the long-run impacts of each of the \( n \) residuals in \( u_t \). Accordingly, the long-run matrix associated to the fundamental shocks \( e_t \) results as \( \Xi := \Xi^* B. \) In detail, the elements of this matrix equal the structural impulse responses that are reached when the adjustment processes following a shock are finished.

Once the structural coefficients are identified, they provide the basis for the impulse response analysis which will be presented in section 5. In the following, we discuss the long-run restrictions imposed in order to disentangle the structural shocks of interest. As pointed out above, 10 linearly independent restrictions either in \( B \) or in \( \Xi \) are needed to exactly identify the model. We define \( \xi_{i,j} \) as the long-term effect of the \( i \)th variable on the \( j \)th structural shock. For the moment, we implement only long-run restrictions to identify the structural shocks.\(^7\)

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\(^5\) In some of our robustness checks below, identification is obtained through a combination of short- and long-run constraints.

\(^7\) Also Balleer and van Rens (2013), for instance, avoid short-term restrictions to identify SBTC. They argue that the assumption that wages are proportional to marginal products might not hold in the short run if there are frictions in the wage determination process.
Essentially, we are only interested in the effects of technology shocks, SBT shocks and inequality shocks. For the time being, the remaining two shocks are identified as labour demand and supply, disentangling them by the standard neoclassical assumption $\xi_{h,w} = 0$. However, in a robustness check, we also simply leave the correlation of the $w$- and $h$-residuals unidentified. In any case, the two shocks are assumed to have no long-run impact on productivity ($p$) and relative skill productivity ($SBTC$). This is in line with the standards in the growth literature stating that the only relevant long-term drivers of productivity are technology shocks.

A crucial variable of interest is inequality that is defined as being affected only by its own shocks and – since SBTC is a potential source of $I$ – by SBT shocks. Structural inequality shocks can occur, for instance, through changes in the employers’ hiring preferences that lead to substandard employment, the introduction or changes of minimum wages, through de-regulation of temporary employment, or through labour market reforms in general (e.g. the Hartz reforms, compare Klinger and Weber (2016)). Furthermore, globalisation or outsourcing (which are not necessarily linked to technological change) surely have their impact on inequality, if they favour workers in exporting sectors more than those in non-exporting sectors. In sum, on the present model’s level of aggregation, inequality-driving forces are divided into SBTC and structural inequality shocks, where the latter comprise inequality-relevant factors. Of course, not all of these factors will have exactly identical economic effects, but we aim at identifying an overall effect of inequality. Even if one of its factors should have effects strongly different from the overall shock, then at least we can say that this factor cannot be quantitatively important.

By contrast, $SBTC$ is defined as being driven only by SBT shocks. Examples could be the widespread usage of computers or robotics at workplaces or other skill-complementing or low-skill replacing technologies. This is in line with explicitly modelling SBTC as source of inequality, the reasoning followed in our modelling framework. Notwithstanding, the constraint $\xi_{SBTC,I} = 0$ could be questioned if a higher endowment with high-education workers – also connected to higher inequality ceteris paribus – leads to a bigger market for skill-biased technologies in the long run (i.e., directed technical change, compare Acemoglu i998)). Therefore below we run robustness checks on the involved restriction.

The third shock of interest is the normal, i.e. skill-neutral, technology shock. This shock is defined as having no long-run impact on SBTC and on inequality which yields the two remaining constraints required for identification. To summarize, the restrictions read as follows:

$$
\Xi = \begin{pmatrix}
\xi_{p,p} & 0 & 0 & \xi_{p,SBT} & \xi_{p,I} \\
\xi_{w,p} & \xi_{w,w} & \xi_{w,h} & \xi_{w,SBT} & \xi_{w,I} \\
\xi_{h,p} & 0 & \xi_{h,h} & \xi_{h,SBT} & \xi_{h,I} \\
0 & 0 & \xi_{SBTC,SBT} & 0 \\
0 & 0 & \xi_{I,SBT} & \xi_{I,I}
\end{pmatrix}.
$$

(9)
4.3 Estimation

Estimation of Equation (6) requires some further discussion. First, we choose the optimal lag length according to the Akaike Information Criterion (AIC) and find \(q = 2\). Second, we try to keep the model as parsimonious as possible by sequentially excluding the elements in the adjustment vector \(\alpha\) and in \(A_i\) of lagged endogenous variables that lead to worse AIC values. Third, as mentioned in section 3, we allow for an economically motivated cointegration relation between \(p\) and \(w\).

The estimation method involves two stages (compare, e.g., Lütkepohl (2005)). In the first stage, \(\beta\) is estimated. The equation is then estimated by OLS and the cointegration relation is extracted by normalizing the coefficient of the first variable \((p)\) to 1. In the second stage, the restrictions on the elements of \(A_i\) can be accounted for. The term \(\beta'_y y_{t-1}\) is treated as an additional variable. Due to the constraints in \(A_i\), the set of regressors is not the same in each of the equations which would lead to inefficient estimates in case of OLS. As a consequence, the white noise covariance matrix \(\Sigma_u\) is used to compute a GLS-type estimator. Applying LM-tests, no evidence of remaining residual autocorrelation was found.

After obtaining the dynamics of the model from the reduced form (Equation (6)), the structural form is estimated by maximum likelihood given the restrictions in Equation (9).

5 Results

5.1 Impulse Responses

From the structural model, we estimate impulse responses and confidence intervals using the bootstrap of Hall (1992) with 2,000 replications. Figures 5 to 7 show the impulse responses for a horizon of 16 quarters together with 2/3 confidence intervals. We consider 1 unit shocks. As all variables were multiplied by 100, this implies a technology shock connected to an immediate 1 percent productivity impact, an SBT shock connected to an immediate 1 percent impact on SBTC (i.e., the relation of the factor-augmenting technology terms of the high- and low-skilled) and an inequality shock connected to an immediate impact of 1 point on the Gini coefficient (scaled between 0 and 100).

As expected, skill-biased technology shocks increase productivity (Figure 6, upper panel). Along with productivity, also wage costs rise (middle panel). However, hours worked are clearly reduced by the SBT shock (lower panel). This is consistent with high-skilled workers being more productive than low-skilled workers: Then, if the relative demand for high-skilled is increased, less hours are required for producing a given output. There is only a weak rebound visible in the impulse response, which could reflect reallocation of labour following an initially distortionary shock. In this context, one might hypothesise that adjustment to technical change in the German labour market has been limited due to sclerotic structures. However, the labour market reforms in 2003-2005 could have changed this by improving flexibility and reallocation capacity. Indeed, when estimating the model only until 2002,
Figure 5: Responses of $p$, $w$ and $h$ to technology shocks

Notes: The solid line shows the responses of productivity (upper panel), wage cost (middle panel) and hours (lower panel) to 1% (skill-neutral) technology shocks up to 16 quarters. The dotted line denotes Hall (1992)’s 2/3 bootstrapped confidence interval. Source: Own calculations.
Notes: The solid line shows the responses of productivity (upper panel), wage cost (middle panel) and hours (lower panel) to 1% SBT shocks up to 16 quarters. The dotted line denotes Hall (1992)'s 2/3 bootstrapped confidence interval.
Source: Own calculations.
Figure 7: Responses of $p$, $w$ and $h$ to inequality shocks

Notes: The solid line shows the responses of productivity (upper panel), wage cost (middle panel) and hours (lower panel) to 1 unit inequality shocks up to 16 quarters. The dotted line denotes Hall (1992.)'s 2/3 bootstrapped confidence interval. Source: Own calculations.
we measure an even more negative hours reaction to SBT shocks without any rebound. Logically, the period after the reforms is inclined to more advantageous SBT effects.

As expected, inequality is positively affected by SBT shocks (Figure 8). This confirms the role of SBTC as source of inequality and can be taken as a plausibility check for our identification scheme. A 1 percent shock to SBTC increases the Gini coefficient (scaled between 0 and 100) by about 0.012. While this value seems rather limited, the large range of the SBTC variable over the sample (Figure 3) compared to the other variables must be taken into account.

(Skill-neutral) technology shocks naturally increase productivity and wages (Figure 5, upper and middle panels), the latter partly with delay. Notably, we also find an increase for hours worked (lower panel). This positive effect following a 1 percent technology shock is weak in the short run but increases in the following until about 0.4 percent. It stands in contrast to the persistent negative effects reported in Gali (1999) and subsequent literature. In this context, note that these latter results are based on a single technology shock that implicitly captures both skill-neutral and skill-biased technology shocks (compare also Balleer and van Rens (2013)). The hours effect of the latter has already been shown to be negative above. Logically, responses to overall (intermingled) technology shocks will incline more towards the negative area. Indeed, if we eliminate SBTC and inequality from the system and thus estimate a small standard model, the response of hours to the technology shock is negative on impact and insignificant in the following. However, the positive hours effect reached in the complete model is more in line with the expectation from standard search and matching theory that plain productivity shocks foster vacancy creation and therefore employment.

As SBTC, structural inequality shocks have a negative impact on hours worked (Figure 7, lower panel). In addition, they reduce productivity (upper panel) and wage costs (middle panel). These variables drop by 0.5 to 0.6 percent, hours by just under half as much.
following a shock of one point in the Gini coefficient scaled between 0 and 100. This implies that relevantly sized employment and productivity impacts appeared in the past: Recall Figure 4 that shows a range of about 5 points for the Gini coefficient over the sample. The results indicate that inequality has adverse impacts on the labour market as implied by theories in line with the opportunities hypothesis. Moreover, there appear to be no counterbalancing effects in terms of efficiency (i.e., productivity) gains, quite the contrary.

In sum, the investigation implies that higher inequality harms employment and productivity in Germany. Naturally, as in all empirical models, these results must not be extrapolated too far beyond the range of observed data. For instance, one cannot infer that complete equality would bring about the most beneficial effects.

5.2 Upper and Lower Inequality

**Figure 9: Inequality above and below the median wage**

Notes: The graph shows the seasonally adjusted Gini coefficient below (solid line) and above (dotted line) the median wage based on full time workers subject to social security contributions aged 15 to 64. Level shifts in January 1978, January 1984 and January 1992 have been eliminated. The monthly data were converted to quarterly frequency. Further information in the text.
Source: IEB.

A comparison of the respective origins of the incentive hypothesis and the opportunities hypothesis leads to the conclusion that the latter has been designed mainly for developing countries since it explicitly addresses the opportunities of *the poor*. Barro (2000) and Castelló-Climent (2010), for instance, investigate the effects of inequality on growth separately for rich and poor countries and find the relationship to be positive in the former and negative in the latter. Transferred into the context of industrialized countries, this could
imply that the two contradicting hypotheses are not equally important in different parts of the wage distribution (see, e.g., Voitchovsky (2005)).

**Figure 10: Responses of \( p, w \) and \( h \) to \( I_l \)-shocks**

**Notes:** The solid line shows the responses of productivity (top), wage inequality (middle), and hours (bottom) to 1 unit shocks in wage inequality below the median wage up to 16 quarters. The dotted line denotes Hall (1992)’s 2/3 bootstrapped confidence interval. 
*Source:* Own calculations.

In order to shed more light onto this issue, we calculate inequality above (“upper inequality”, \( I_u \)) and below (“low inequality”, \( I_l \)) the median. This is done by applying Equation (4) separately to all individuals earning less \( (I_l) \) or more \( (I_u) \) than the median wage, re-
Figure 11: Responses of $p$, $w$ and $h$ to $I_u$-shocks

Notes: The solid line shows the responses of productivity (top), wage inequality (middle), and hours (bottom) to 1 unit shocks of wage inequality above the median wage up to 16 quarters. The dotted line denotes Hall (1992)’s 2/3 bootstrapped confidence interval. Source: Own calculations.
respectively. Figure 9 shows that the increase in total inequality seems to be driven mainly by an increase in wage dispersion above the median, at least until the mid-nineties, while the marked decrease in inequality since 2010 comes from reduced wage dispersion below the median ($I_l$). The two different dynamics by which total inequality is driven raises the question whether the respective shocks have different impacts in our structural model.

In order to investigate potential differing effects, we add the two inequality variables in our model (in place of overall inequality). Thereby, we model no causal effects between the two inequality measures. While their residuals can be correlated, it appears plausible to trace this correlation back to common factors rather than to bilateral spillover effects. Technically, this is implemented by allowing for correlation between the structural residuals $\epsilon_{I_l}$ and $\epsilon_{I_u}$, which does not influence the impulse responses.

Figures 10 and 11 show the resulting responses to the respective structural shocks. The negative labour market effects of inequality shocks are prevailing for both upper and lower inequality. However, the latter has stronger (negative) effects on productivity, wage costs and hours than overall inequality. An explanation could be connected to the relevance of the opportunities and incentive hypotheses for higher and lower wage groups. The former, postulating that inequality impedes opportunities to participate on educational advancement, points to the situation of low-income workers. Therefore, it is likely to strengthen the adverse effects of lower inequality. In contrast, the incentive hypothesis might be more relevant for higher income jobs, where career paths and development chances are more prevailing. Logically, this would dampen negative effects of $I_u$.

### 5.3 Robustness Analysis

Since we provide evidence for the effects of inequality in a novel econometric framework, robustness checks gain particular importance. We pursue the following steps:

- We change the elasticity of substitution $\sigma$ to 1.4 or to 2.0 when calculating the SBTC time series.
- We drop the neoclassical assumption $\xi_{h,w} = 0$, instead leaving the residuals connected to wage cost and hours unidentified.
- We relax the long-run restriction on the impact of inequality shocks on SBTC and replace it by the respective zero restriction in the short-run matrix $B$. This requires only the weak assumption that the potential triggering of the development of skill-biased technologies according to directed technical change does not pass off within a single quarter.

Figure 12 shows the resulting impulse responses of $p$, $w$ and $h$ to inequality shocks, compared to the baseline model (solid lines) described in section 4. The reactions of $p$ and $w$ are a bit stronger when using $\sigma = 1.4$ for measuring SBTC (dotted lines) or when allowing for directed technical change (triangles). The reactions of $h$ are marginally weaker for $\sigma = 2.0$ (dashed lines) and for the setting with directed technical change and – again – a bit stronger for $\sigma = 1.4$. The reactions are virtually unaffected by dropping the neoclassical assumption $\xi_{h,w} = 0$ (cross symbols). In total, Figure 12 shows that our results are rather robust to alternative settings and identification schemes.
Figure 12: Robustness checks: Responses of $p$, $w$ and $h$ to inequality shocks

Notes: The graphs show robustness checks with respect to the responses of $p$, $w$ and $h$ to 1 unit inequality shocks up to 16 quarters. See text for more details.
Source: Own calculations.
6 Conclusion

In the underlying study we analysed the effects of inequality and skill-biased technical change (SBTC) on the economy and the labour market. We explicitly model SBTC as source of inequality to isolate structural inequality shocks. We put forward a dynamic cointegrating framework with theory-based (short- and) long-run restrictions for identifying the impacts of inequality on productivity, wage costs and hours worked.

A structural impulse response analysis revealed that skill-biased technology shocks increase productivity and wage costs, but reduce hours worked and raise inequality. Structural inequality shocks also have a negative impact on hours worked, but additionally reduce productivity. We find that inequality both above and below the median wage have negative labour market effects, somewhat stronger for the former. Furthermore, by separating skill-biased technology shocks, we can show that skill-neutral technology shocks have a positive long-run effect on hours worked. In general, the results indicate that inequality has negative long-run impacts on the labour market as implied by theories in line with the opportunities hypothesis. Moreover, there appear to be no counterbalancing effects in terms of efficiency (i.e., productivity) gains, quite the contrary.

The results imply that the rising wage inequality in Germany since the 1990s should not be seen as a precondition for the German labour market upswing of the recent ten years. Instead, higher inequality appears to harm employment and productivity. The employment upswing is more likely connected to those components of the reforms that aimed at enhancing the efficiency of the labour market functioning (compare Klinger and Weber (2016)) as well as to other factors such as the upward trend of the service sector and high immigration in recent years (e.g Klinger and Weber (2015)). Wage moderation as such could also have played a role in strengthening labour demand, but according to our analysis wage inequality was an obstacle to labour market development. However, the development of declining inequality since the end of the Great recession – in addition to a lower mismatch between unemployed and vacancies (Hutter and Weber (2017)) – is likely to have contributed to expanding employment during a period where a lowering speed due to the phasing-out of the Hartz-reform effects was already expected.

Furthermore, the results on SBTC can be taken as a warning signal for the current wave of – intelligent and interconnected – digitalisation ("4.0"). According to research results for Germany, this will raise the qualification needs (Wolter et al. (2016)). As far as the development is connected to an essentially skill-biased technical change, there appears to be a risk of negative employment effects. This underlines the key role of qualification.

The general construction of the model framework paves the way for further economic analyses of inequality. Measuring economic effects of inequality based on data from other countries could shed light on the degree of generality or conditionality of the results. Moreover, the functional form could be extended in order to capture potential nonlinearities in the relationship of inequality and labour market outcomes. Finally, additional differentiation in modelling inequality shocks could elaborate further on the concrete mechanisms at work.
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